

DETECTION OF A DEARTH OF STARS WITH ZERO ANGULAR MOMENTUM IN THE SOLAR NEIGHBOURHOOD

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ABSTRACT

We report on the detection in the combined *Gaia*-DR1/RAVE data of a lack of disk stars in the solar neighbourhood with velocities close to zero angular momentum. We propose that this may be caused by the scattering of stars with very low angular momentum onto chaotic, halo-type orbits when they pass through the Galactic nucleus. We model the effect in a Milky-Way like potential and fit the resulting model directly to the data, finding a likelihood ($\sim 2.7\sigma$) of a dip in the distribution. Using this effect, we can make a dynamical measurement of the Solar rotation velocity around the Galactic center: $v_{\odot} = 239 \pm 9 \text{ km s}^{-1}$. Combined with the measured proper motion of Sgr A*, this measurement gives a measurement of the distance to the Galactic centre: $R_0 = 7.9 \pm 0.3 \text{ kpc}$.

Subject headings: Galaxy: disk — Galaxy: fundamental parameters — Galaxy: kinematics and dynamics — Galaxy: nucleus — solar neighborhood — stars: kinematics and dynamics

1. INTRODUCTION

We are entering a golden age for Milky Way astronomy. The European Space Agency (ESA)’s *Gaia* mission (Gaia Collaboration et al. 2016a), which launched 19th December 2013, has recently published its first data release (Gaia Collaboration et al. 2016b), giving us a new window on our Galaxy, and in particular, the solar neighbourhood. The primary astrometric catalogue in *Gaia*-DR1 is the Tycho-*Gaia* Astrometric Solution (TGAS, Michalik et al. 2015; Lindegren et al. 2016), which uses data from the *Tycho*-2 catalogue (Høg et al. 2000), to provide a baseline of approximately 30 years upon which to calculate astrometric values for stars in common between *Tycho*-2 and *Gaia*. There is also significant overlap between stars in the TGAS catalogue and stars observed by the Radial Velocity Experiment (RAVE, e.g. Steinmetz et al. 2006), enabling the full 6-dimensional phase space information to be known for over 200,000 stars in the solar neighbourhood. This enables us to explore local dynamics in unprecedented detail.

Many aspects of the structure and dynamics of the Milky Way are difficult to measure, owing to our position within the Galaxy, and complex observational selection effects such as dust extinction. Thus, many of the fundamental parameters of the Milky Way carry significant uncertainty. One such parameter is the velocity at which the Sun rotates around the Galaxy, for which plausible values span the range from $\approx 240 \text{ km s}^{-1}$ to 260 km s^{-1} (e.g., Bovy et al. 2012; Reid et al. 2014) and are dependent on the data set and technique used.

Carlberg & Innanen (1987) proposed that the rotation velocity of the Sun may be measured by searching for a lack of stars exhibiting zero angular momentum⁴. Stars with zero angular momenta are expected to plunge

into the Galactic nucleus and subsequently experience scattering onto chaotic orbits with a high scale height, henceforth spending the majority of their time in the stellar halo (Martinet 1974). If stars with very low angular momentum are indeed not present in the solar neighbourhood, the tail of the tangential velocity distribution will exhibit a dip centred at the Solar reflex value. This method for measuring the Solar velocity is attractive because it should depend only on the existence of low angular momentum orbits within the Milky Way’s disk. With 6-dimensional phase space measurements for nearby stars it becomes possible to calculate the tangential velocity distribution with respect to the Sun, and thus we can test this prediction by searching for a dearth of stars around the assumed value of the negative of the Solar motion.

This paper is constructed as follows. In Section 2 we discuss our treatment of the data, and the feature observed in the resulting velocity distribution. In Section 3 we present simulated models which can explain the feature and make predictions for the size and shape of the observed feature. In Section 4 we fit our model to the data and present our measurement of $v_{\odot, \text{reflex}}$. Finally, in Section 5 we discuss the implications of the detection and look forward to future measurements.

2. OBSERVED FEATURE

We cross match the TGAS catalogue (Lindegren et al. 2016) and the RAVE DR5 data (Kunder et al. 2016) to add RAVE line-of-sight velocities to the TGAS astrometric data. Where available, we employ the RAVE spectrophotometric distance estimates, because estimating distances from the TGAS parallax is non-trivial (e.g. Bailer-Jones 2015). However, where no RAVE distance is available, we naively invert the TGAS parallax π to obtain distance estimates for the remaining stars, removing any star with $\sigma_{\pi}/\pi > 0.1$ to avoid large distance uncertainties. The resulting sample consists of 216,201 stars

velocities with respect to the Sun, the quantity that is directly measured is the Sun’s motion around the center, not the circular velocity. The difference between these two is still quite uncertain (e.g., Schönrich et al. 2010; Bovy et al. 2015)

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⁴ Carlberg & Innanen (1987) phrased this as a measurement of the circular velocity. Because the measurement is based on stellar

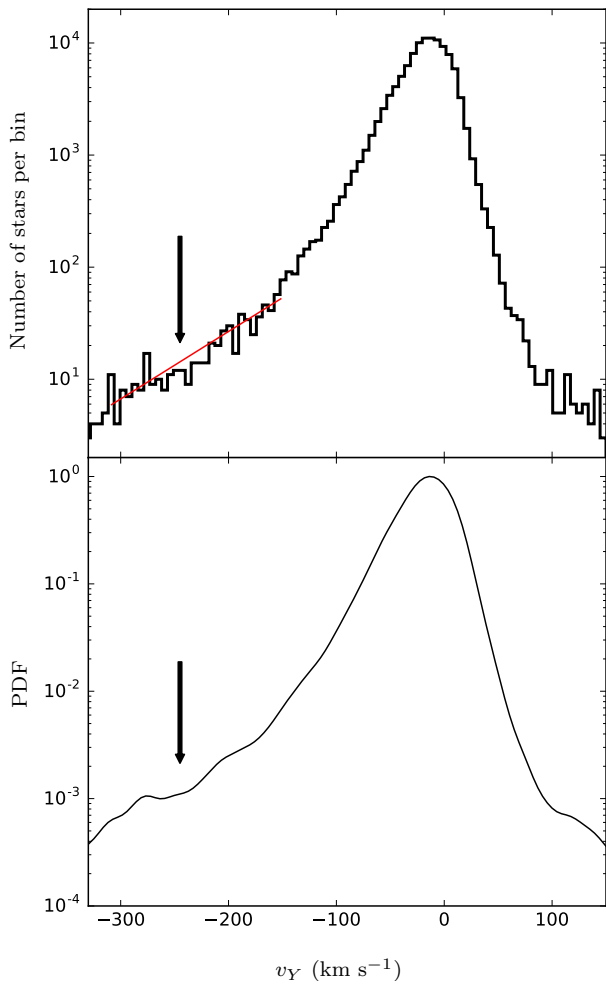


FIG. 1.— **Top panel:** Distribution of v_Y for stars observed to be within 700 pc of the Sun. The Sun’s velocity has $v_Y = 0$. The low-velocity tail of the distribution displays a clear dip in the range between -210 km s^{-1} and -270 km s^{-1} that is marked with an arrow and overlaid with an exponential for illustration. **Bottom panel:** Normalised KDE of the above distribution clearly showing the dip.

with 6-dimensional phase-space measurements. Then, we convert the velocities from equatorial coordinates to standard Galactic Cartesian coordinates centred on the Sun, (X, Y, Z, v_X, v_Y, v_Z) , with v_X positive in the direction of the Galactic centre (toward Galactic longitude $l = 0$) and v_Y positive in the direction of Galactic rotation (toward $l = 90^\circ$), both measured with respect to the Sun.

Figure 1 shows the distribution of v_Y for stars within 700 pc as a histogram (top panel) and with Kernel Density Estimation (e.g., Wasserman 2006; bottom panel) using a Gaussian kernel with bandwidth 9. We chose 700 pc as a balance between quantity of stars, and quality of data. There is a clear underdensity of stars in the approximate region of -210 km s^{-1} to -270 km s^{-1} , marked with an arrow (see also the top panel of Figure 4).

Although there are only ≈ 10 stars per bin at these velocities, this dip in the distribution is clear across ≈ 8 bins. We defer a discussion of the significance of the dip until Section 4 where we fit a model for the dip obtained from simulations.

Furthermore, in the two-dimensional distribution of (v_X, v_Y) , we find a lack of stars with both positive v_X and large negative v_Y . That is, there are very few stars observed on disk orbits ($|v_X| < 150 \text{ km s}^{-1}$ and $|v_Z| < 150 \text{ km s}^{-1}$) plunging towards the Galactic centre. Quantitatively, there are 24 stars with $v_X > 0$ in the range $-290 \text{ km s}^{-1} < v_Y < -230 \text{ km s}^{-1}$ and 34 stars with $v_X < 0$. These rates are inconsistent with being drawn from the same distribution at $\gtrsim 1.7\sigma$.

Our analysis does not explicitly take into account the uncertainties on the distance or velocity estimates. Propagating the uncertainties through the coordinate transformation results in an uncertainty of approximately 10 per cent on the measured cartesian velocities. At the v_Y range of the dip, this corresponds to uncertainties of approximately 24 km s^{-1} . Because the width of the dip feature appears to be approximately 60 km s^{-1} we can neglect the uncertainties in this initial investigation.

3. EXPECTATION FROM GALACTIC MODELS

A likely explanation for these missing stars, as mentioned in Section 1, is that they have been scattered onto chaotic orbits with larger scale heights by interaction with the Galactic nucleus. This is expected for disk stars with approximately zero angular momentum as discussed in Carlberg & Innanen (1987). Thus, as these stars would then spend the majority of their orbits far from the Galactic plane, it is very unlikely that they would be observed in the solar neighbourhood at any one given time. In Galactocentric coordinates, such stars have tangential velocities $v_T \approx 0$, corresponding to heliocentric $v_Y \approx v_{\odot, \text{reflex}}$, minus the Solar tangential velocity measured in the Galactocentric frame.

Carlberg & Innanen (1987) performed an analysis of this effect and matched models of the dip constructed within an analytic potential to data from local stellar catalogues complete to 25 pc. They found the dip to be centred at 250 km s^{-1} , with a depth greater than 80%. However, they are careful to note that there are only 18 stars with $v_Y < -140 \text{ km s}^{-1}$ and that a larger sample will improve the measurement. The TGAS+RAVE sample used here has $374 \text{ stars with } -310 \text{ km s}^{-1} \leq v_Y < -150 \text{ km s}^{-1}$, allowing far greater confidence in our subsequent analysis of the feature.

Firstly, we make a fresh prediction of the feature which we expect to observe in the TGAS data, similar to Carlberg & Innanen (1987), but with an updated potential, and drawing the distribution of initial positions, radial, and vertical velocities from the observed data to tailor the prediction to the current data set. It is challenging to construct an N -body model with sufficient resolution to predict the high velocity tail in the local neighbourhood. Thus, we integrate test particles in a Milky-Way like potential, and observe the resulting orbits.

For our Milky-Way potential we use `MWPotential2014` from `galpy` (Bovy 2015). `MWPotential2014` consists of a power-law spherical bulge potential with an exponential cut-off, a Miyamoto-Nagai disk potential, and a

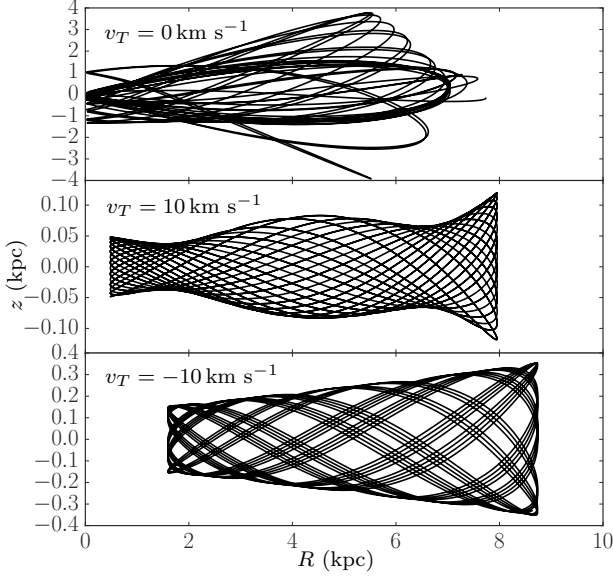


FIG. 2.— **Top panel:** Example orbit of a particle with $v_T = 0 \text{ km s}^{-1}$ exhibiting chaotic behaviour. **Middle panel:** Example orbit of a particle with $v_T = 10 \text{ km s}^{-1}$. **Bottom panel:** Example orbit of a particle with $v_T = -10 \text{ km s}^{-1}$. Orbits that penetrate the galactic nucleus are scattered onto non-disk orbits that spend little time in the solar neighborhood.

NFW halo potential. The parameters of this potential have been fit to a wide variety of dynamical data in the Milky Way; the full parameters are given in Bovy (2015). To model the hard Galactic nucleus that is not included in MWPotential2014, we also include a Plummer potential $\Phi(R, z) = -M/\sqrt{R^2 + z^2 + b^2}$, where $M = 2 \times 10^9 M_\odot$ and $b = 250 \text{ pc}$. Note that we do not include a non-axisymmetric bar potential in this initial work, which may affect the feature slightly. This should be considered when applying this technique to future *Gaia* data releases.

Figure 2 displays the orbits of three stars integrated for 2 Gyr. The top panel shows the orbit of a star with $v_T = 0 \text{ km s}^{-1}$, which exhibits chaotic behaviour upon interaction with the galactic nucleus. The middle and lower panels show the orbits of stars with $v_T = 10 \text{ km s}^{-1}$ and $v_T = -10 \text{ km s}^{-1}$, respectively, which exhibit well-behaved disk orbits. The star with no angular momentum spends little of its orbital period near the galactic plane, whereas the two stars which do not approach the nucleus remain within a few hundred parsecs of the plane.

Without an ab-initio model for the disc, it is difficult to predict how many stars are expected to be missing near zero angular momentum and what the exact profile of the dip should be. Therefore, we use the fraction of the orbital period of the test-particle stars that they spend near the mid-plane of the disc as a proxy for whether it has been scattered to a much higher scale height. We integrate many orbits with positions, radial, and vertical velocities drawn from the TGAS+RAVE sample and from an initial, uniform distribution in v_Y covering the low-velocity tail. We then re-weight the stars using the

fraction of time they spend near the plane and construct the dip profile by dividing this weighted, final v_Y distribution by the initial, uniform distribution.

Figure 3 shows the computed dip profiles for velocities within 80 km s^{-1} of $v_T = 0$. The top panel shows the results of 7 simulations with reflex solar motion, $v_{\odot, \text{reflex}}$, of $-220, -230, -235, -240, -245, -250$ and -260 km s^{-1} , assuming $|z| < 300 \text{ pc}$ as the criterium ‘close to the disc plane’. It is clear that the shape and depth of the overlaid distributions are very similar and thus not dependent on the value of the solar motion. The dip profile is not entirely symmetric around zero $v_Y - v_{\odot, \text{reflex}}$, because the spatial distribution of the TGAS+RAVE sample is asymmetric around the Sun. The middle panel of Figure 3 displays the same as the upper panel, for $v_{\odot, \text{reflex}} = -240 \text{ km s}^{-1}$, but assuming $|z| < 1 \text{ kpc}$ to weight the orbits. The profile of the dip is notably shallower, with a depth of ~ 0.85 , compared to ~ 0.7 for the models in the top panel, but the shape of the dip profile is similar. The bottom panel of Figure 3 shows same as the middle panel, but assuming $|z| < 50 \text{ pc}$ to weight the orbits. The depth is consistent with the models in the top panel.

We create a function $D(v_Y - v_{\odot, \text{reflex}})$ of the dip by smoothly interpolating the model with $v_{\odot, \text{reflex}} = -240 \text{ km s}^{-1}$ and $|z| < 300 \text{ pc}$ displayed in the top panel of Figure 3. Because the dip profile computed above is an approximation, we give the model more freedom by allowing the dip’s amplitude to vary. We model the full distribution $f(v_Y)$ of v_Y as an exponential multiplied by the dip:

$$f(v_Y) \propto \exp(m v_Y + b) \times \left(1 - \alpha \left[\frac{1 - D(v_Y - v_{\odot, \text{reflex}})}{1 - D(0)} \right] \right). \quad (1)$$

Written in this manner, the depth is parameterized by a parameter α , normalized such that $\alpha = 0$ corresponds to no dip and $\alpha = 1$ corresponds to a dip reaching all the way to zero, i.e., a complete absence of stars.

4. DETECTION OF A ZERO-ANGULAR-MOMENTUM FEATURE IN *GAIA*-DR1

We fit the distribution of v_Y of disk stars ($|v_X| < 150 \text{ km s}^{-1}$ and $|v_Z| < 150 \text{ km s}^{-1}$) in the range $-310 \text{ km s}^{-1} \leq v_Y < -150 \text{ km s}^{-1}$ using the model in Equation (1). The top panel of Figure 4 displays the best fit $\alpha = 0$ model overlaid on the zoomed in tail of the histogram of the distribution of v_Y . This clearly demonstrates the dearth of stars between approximately $v_Y = -210 \text{ km s}^{-1}$ and -270 km s^{-1} when compared with the exponential model.

The best-fitting dip model is shown in the bottom panel of Figure 4. The data prefer a dip: the log likelihood of the best-fit model is $\ln \mathcal{L} = 282.0$, compared with $\ln \mathcal{L} = 276.7$ for the best-fit exponential model with two fewer parameters ($\alpha = 0$). For comparison, we also fit a model where we allow the width to be controlled by a new parameter w that stretches the profile in Figure 3 along the x axis. For this model we find $\ln \mathcal{L} = 282.7$ and $w = 1.8$. Although the likelihood is marginally higher for this model, the significance of the detection is lower ow-

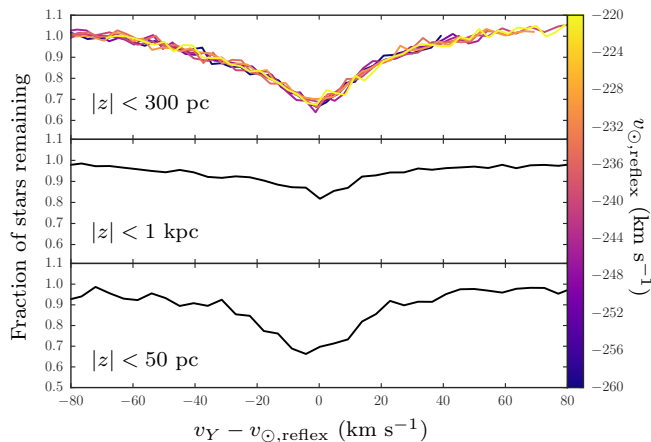


FIG. 3.— **Top panel:** Fraction of stars remaining in stable orbits with initial velocities close to $v_T = 0 \text{ km s}^{-1}$ for seven simulations in the range $v_{\odot, \text{reflex}} = -220$ to -260 km s^{-1} . **Middle panel:** Same as top panel, but for $|z| < 1 \text{ kpc}$. **Bottom panel:** Same as top panel, but for $|z| < 50 \text{ pc}$.

ing to the extra free parameter.

Using the Akaike information criterion (AIC, Akaike 1974) the difference in \ln likelihood corresponds to a 2.1σ detection for the $w = 1$ model and a 1.8σ detection for the w free case. When combined with the 1.7σ detection from the v_X to v_Y analysis using a Bonferroni correction to account for the multiple tests (e.g. Dunn 1959) this gives a 2.7σ detection for $w = 1$ and a 2.5σ detection when w is left free. We explore the allowed range of models for $w = 1$ using a Markov Chain Monte Carlo (MCMC) analysis with *emcee* (Foreman-Mackey et al. 2013). We find that $\alpha = 0.52 \pm 0.1$ and $v_{\odot, \text{reflex}} = -239 \pm 9 \text{ km s}^{-1}$ at 1σ .

Even though we do not have an ab-initio prediction of the dip profile, we find that the best-fitting α is consistent within its uncertainty to that obtained using the models (which have $\alpha \approx 0.3$). Thus, systematics due to our approximate model for the dip in a simple axisymmetric Milky-Way potential are likely quite small.

5. DISCUSSION AND OUTLOOK

We have shown that a dip in the low-velocity tail of stars in the solar neighborhood is present at 2.7σ significance. This feature can be plausibly explained by the absence of stars on orbits with approximately zero angular momentum, due to such stars being scattered onto halo orbits after interaction with the Galactic nucleus as predicted by Carlberg & Innanen (1987). Using orbit integration in a realistic model of the Galactic potential, we have demonstrated that this dip should be centered on minus the Solar rotational velocity $v_{\odot, \text{reflex}} = -v_{\odot}$. In this way, we were able to measure $v_{\odot} = 239 \pm 9 \text{ km s}^{-1}$. Our modeling does not include the Galactic bar or spiral arms, which affect the orbits of stars. However, because the dip is due to zero-angular momentum stars moving on orbits that are highly eccentric that are being lost from the solar neighborhood over many dynamical times, the gravitational perturbations and current position of the relatively diffuse stellar bar and of the spiral structure should not greatly affect the profile of the dip and we

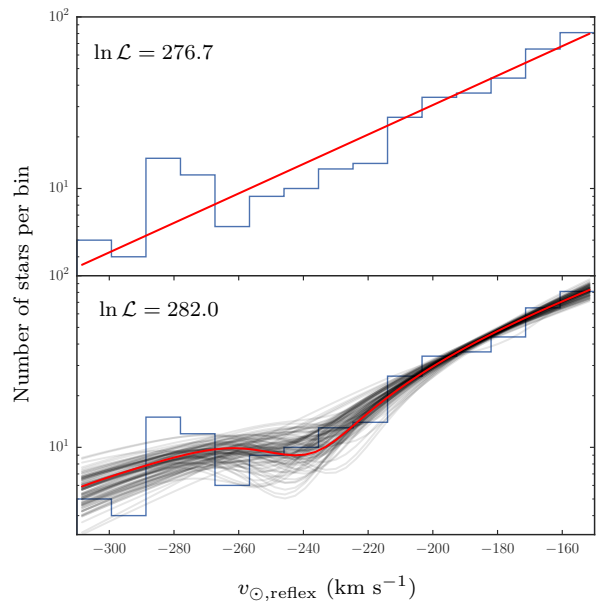


FIG. 4.— **Top panel:** Tail of the v_Y distribution overlaid with the best fit model assuming $\alpha = 0$. **Bottom panel:** Tail of the v_Y distribution overlaid with the best fit model (red) allowing the dip depth α to be a free parameter. We also display 100 models randomly sampled for the parameters from MCMC. Each panel includes the \ln likelihood of the best-fit. The dip is detected at 2.1σ and centered on -239 km s^{-1} .

expect their effect to be minor on our derived value of $v_{\odot, \text{reflex}}$.

Observations of the Galactic center have precisely measured the proper motion $\mu_{\text{Sgr A}^*}$ of Sgr A* (Reid & Brunthaler 2004). Assuming that Sgr A* is at rest with respect to the dynamical center of the Milky Way, this apparent proper motion is due to the reflex motion of the Sun. The ratio of the linear and angular measurements of the reflex motion of the Sun $v_{\odot, \text{reflex}}/\mu_{\text{Sgr A}^*}$ then becomes a measurement of the distance R_0 to the Galactic centre. For $\mu_{\text{Sgr A}^*} = 30.24 \pm 0.11 \text{ km s}^{-1} \text{ kpc}^{-1}$, our measurement of $v_{\odot, \text{reflex}}$ implies $R_0 = 7.9 \pm 0.3 \text{ kpc}$. This is an essentially dynamical measurement of R_0 . If the lack of zero angular momentum stars is confirmed in future *Gaia* data releases and systematics can be controlled, this feature can in principle saturate the precision implied by the uncertainty in $\mu_{\text{Sgr A}^*}$, which is $\approx 30 \text{ pc}$.

Future *Gaia* data releases will have many orders of magnitude more stars, with substantially higher accuracy on the measured parameters. Additionally, future *Gaia* data releases will contain line-of-sight velocities for stars in the Solar neighbourhood, removing the asymmetry in the sample introduced by the necessity to cross match with RAVE. Thus, with future *Gaia* data releases we hope that this technique may provide a very precise measurement of the solar reflex motion with respect to the Galactic centre. We can make a rough prediction for the strength of the feature expected in future *Gaia* data releases by using the *Gaia* Object Generator (GOG, Luri et al. 2014) based on the *Gaia* Universe Model Snapshot (GUMS, Robin et al. 2012). GOG predicts that approximately 17.5 million stars will be observed with radial ve-

locities within 700 pc, and thus, by weighting that number by the fraction of stars in the tail compared to the full sample matched with RAVE, e.g. $374/216,201=0.0017$, we can predict that *Gaia* will observe roughly 30,000 stars in the tail within 700 pc. This should allow us to confirm the existence of this feature, and if present allow us to increase the precision of the measurement of $v_{\odot, \text{reflex}}$ to within approximately 1 km s^{-1} , assuming the errors decrease on the order of \sqrt{N} . In turn the error on R_0 would become dominated by the error in the proper motion measurement. At this level the systematics will then become extremely important, and in future analysis we must take into consideration other factors such as the bar, spiral structure and local giant molecular clouds, although the tangential deflections are expected to be small.

Further work is also needed to fully determine the origin of this feature, and to make more detailed predictions on the shape and depth which we expect to observe. The exact dimensions of the feature are likely slightly dependent on the potential of the inner Galaxy, and thus matching the observed shape in future *Gaia* data releases to dip functions constructed from various models for the

potential may give us valuable insight into the potential of the inner Galaxy.

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